

7.1 Simple and Compound Interest

Simple Interest: interest is earned only on the original investment

Simple Interest Formulas:

$$I = Prt \quad A = P + I$$

where A = amount at the end of investment (\$)

P = Principal or original amount (\$)

r = rate of interest per year (decimal)

t = time invested (years)

I = total interest earned (\$)

Ex. 1 Norma invests \$900 at 5%/a for 7 years.

- a) How much interest does she earn?
- b) What is the total amount in the account?

a) $I = Prt$
 $= 900(0.05)(7)$
 $= 315$

∴ She earns \$315

b) $A = P + I$
 $= 900 + 315$
 $= 1215$

∴ She has \$1215

Ex. 2 Bahar invests \$100 at 7%/ a for 5 years.

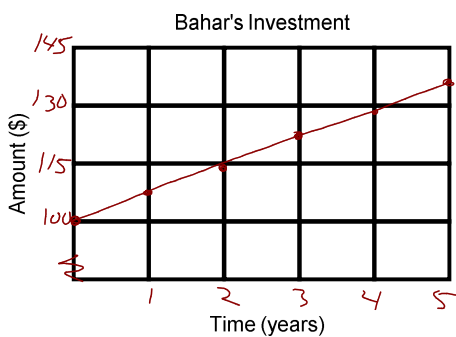
- a) Complete the table to examine what happens to her investment.

Year	Interest	Amount
0		100
1	7	107
2	7	114
3	7	121
4	7	128
5	7	135

What type of sequence does this represent?

- arithmetic seq.
 - linear

- b) Sketch the growth of her money over the 5 years.



What type of growth does this represent?

interest is constant: \$ 7 / yr
 slope is 7

Simple Interest:

- increases by the same amount of money for each time interval.
- creates an arithmetic sequence.
- represents linear growth.

Compound Interest:

- interest is added to the principal for the next compound period
- has the effect of paying/earning interest on interest

Ex. 1 Consider Bahar's investment of \$100 at 7% if the interest is compounded yearly.

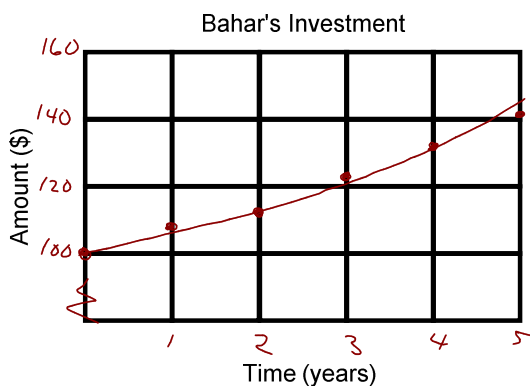
a) Complete the table to examine what happens to her investment.

Year	Interest	Amount
0		100
1	7	107
2	$0.07(107) = 7.49$	114.49
3	8.01	122.50
4	8.58	131.08
5	9.18	140.26

What type of sequence does this represent?

geometric!

b) Sketch the growth of her money over the 5 years.



What type of growth does this represent?

Exponential Growth

amount has a constant ratio
 $r = \underline{1.07}$

Compound Interest:

- increases by a constant multiplier for each compound period.
- creates a geometric sequence.
- represents exponential growth.

Compound Interest Formulas:

note that this is just the formula for exponential growth...the growth factor is $(1 + i)$

$$A = P (1 + i)^n$$

$$I = A - P$$

where P = principal or amount invested/borrowed (\$)
 A = amount at the end of the investment (\$)
 i = interest rate per compound period (decimal)

$$i = \frac{\text{rate}}{\text{\# of compounding periods per year}}$$

n = # of compound periods

$$n = \text{\# of years} \times \text{\# of periods per year}$$

Compounding Periods (how often interest is compounded)

Typical compound periods	annually	1	# of compounds / year
	semi-annually	2	
	quarterly	4	
	monthly	12	
	bi-monthly <i>half month</i>	24	
	bi-weekly <i>every two weeks</i>	26	
	weekly	52	
	daily	365	

Ex. 2 Diane invests \$1500 in an account paying 4.75%/a compounded quarterly. How much money will she have at the end of 5 years?

$$P = 1500$$

$$A = ?$$

$$i = \frac{0.0475}{4}$$

$$n = 5 \times 4 = 20$$

$$A = 1500 \left(1 + \frac{0.0475}{4} \right)^{20}$$

$$= 1899.45$$

\therefore She will have \$1899.45

Ex. 3 Sarah needs to borrow \$4500 to buy her first car. (She is not making payments...she will pay it off in one lump sum in 5 years.)

She has 2 options:

- a) 3.4 %/a for 5 years compounded monthly OR
 b) 3.9%/a for 5 years compounded semi-annually.

Which option is better for Sarah?

$$P = 4500$$

$$a) i = \frac{0.034}{12}$$

$$n = 5 \times 12 = 60$$

$$A = 4500 \left(1 + \frac{0.034}{12} \right)^{60}$$

$$= 5332.59$$

$$b) i = \frac{0.039}{2}$$

$$n = 5 \times 2 = 10$$

$$A = 4500 \left(1 + \frac{0.039}{2} \right)^{10}$$

$$= 5458.64$$

\leftarrow
 \therefore Sarah should choose option A (less to payback)

Ex. 4 Justin has \$24 000 invested in a University fund that he hopes will grow to \$30 000 in 3 years. What interest rate, compounded quarterly will he need to invest at in order to achieve his goal?

$$P = 24000$$

$$A = 30000$$

$$i = ? \left(\frac{i}{4} \right)$$

$$n = 3 \times 4 \\ = 12$$

$$A = P(1+i)^n$$

$$30000 = 24000 \left(1 + \frac{i}{4} \right)^{12}$$

$$1.25 = \left(1 + \frac{i}{4} \right)^{12}$$

$$\sqrt[12]{1.25} = 1 + \frac{i}{4}$$

$$1.01877 = 1 + \frac{i}{4}$$

$$0.01877 = \frac{i}{4}$$

$$i = 0.075$$

\therefore He needs 7.5%/a interest

Simple Interest: Handout "7.1 Simple Interest"

Compound Interest: p. 508 #4, 8-14, 17, 22

