

## 2.1 Key Features of Rational Functions - Part I Reciprocal Functions

A reciprocal function is a function that can be expressed as

$$f(x) = \frac{1}{g(x)} \text{ where } g(x) \text{ is a polynomial function, } g(x) \neq 0.$$

### Example 1

For the following functions state the reciprocal.

a)  $f(x) = x - 3$

b)  $f(x) = (x - 1)(x + 4)$

c)  $f(x) = 16 - x^2$

$$g(x) = \frac{1}{x - 3}$$

$$g(x) = \frac{1}{(x - 1)(x + 4)}$$

$$g(x) = \frac{1}{16 - x^2} = \frac{1}{(4 + x)(4 - x)}$$

Relating the graphs of functions and their reciprocals.

Complete the **Investigation** on pages 248-249

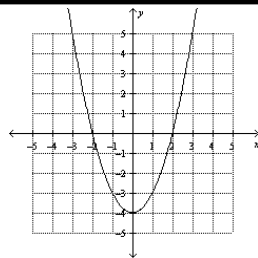
## Handout

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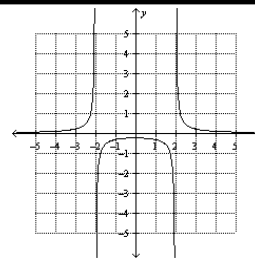
### Example 2

Taken from the Investigation

$$f(x) = x^2 - 4$$



$$g(x) = \frac{1}{x^2 - 4}$$

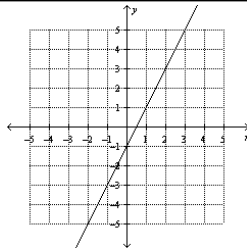


zeros/ asymptotes	Z: $x = -2, 2$ Asym: none	Z: none Asym: $x = -2, x = 2$
$f(x) < 0$	$(-2, 2)$	$(-2, 2)$
$f(x) > 0$	$(-\infty, -2) (2, \infty)$	$(-\infty, -2) (2, \infty)$
$f(x) = -1$	$\pm\sqrt{3}$	$\pm\sqrt{3}$
$f(x) = 1$	same $\pm\sqrt{5}$	same $\pm\sqrt{5}$
decreasing	$(-\infty, 0)$	$(0, \infty), x \neq 2$
increasing	$(0, \infty)$	$(-\infty, 0), x \neq -2$
max/min values	min at $x = 0$	max at $x = 0$

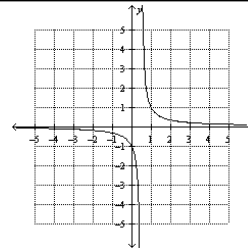
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Example 3

$$f(x) = 2x - 1$$



$$g(x) = \frac{1}{2x - 1}$$

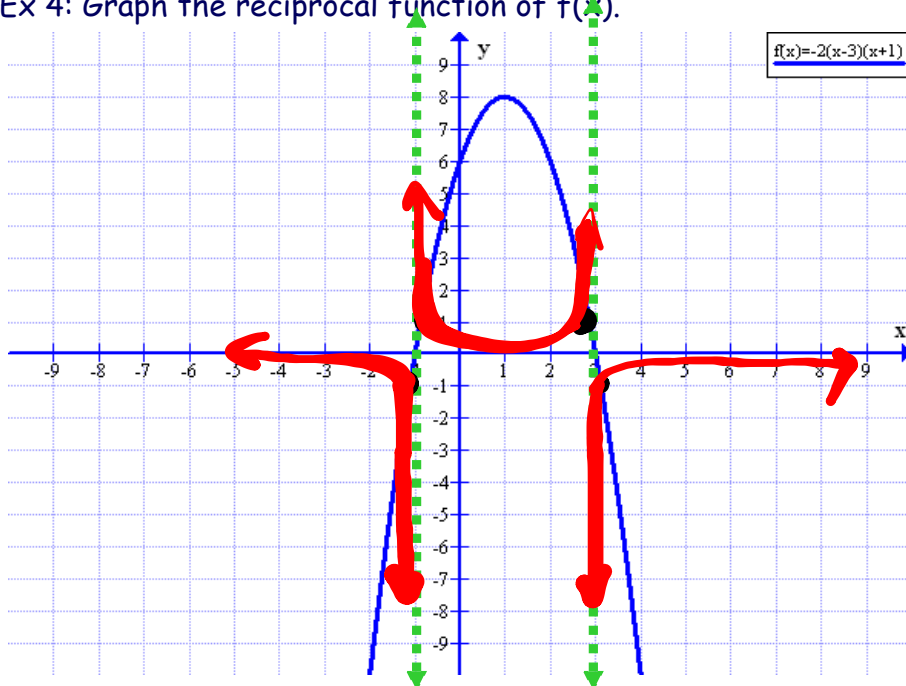


zeros/ asymptotes	Z: $x = 1/2$ Asym: none	Z: none Asym: $x = 1/2$
$f(x) < 0$	$(-\infty, 0.5)$	$(-\infty, 0.5)$
$f(x) > 0$	$(0.5, \infty)$	$(0.5, \infty)$
$f(x) = -1$	$x = 0$	$x = 0$
$f(x) = 1$	$x = 1$	$x = 1$
decreasing	n/a	$(-\infty, \infty), x \neq 0.5$
increasing	$(-\infty, \infty)$	n/a
max/min values	n/a	n/a

*Invariant*

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Ex 4: Graph the reciprocal function of  $f(x)$ .



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**SUMMARY**

Function	Reciprocal Function
Intercepts	become asymptotes
Asymptotes	become zeros
Negative y-values	stay negative
Postive y-values	stay positive
$f(x) = -1$	x value remains the same
$f(x) = 1$	x value remains the same
Increasing	becomes decreasing
Decreasing	becomes increasing
Max/Min Values	switch
The reciprocal function of a linear or quadratic function will always have a horizontal asymptote at $y=0$ .	

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**Homework**

p.254 #  
1,2cd,3,6cd,7a,  
8f,10,11,13,16

*+ factoring worksheet*

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