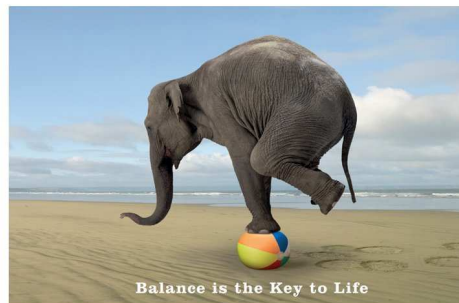


2.7 Solving Inequalities



Recall:

Relational operators are used to express inequalities:

- > greater than
- \geq greater than or equal to
- < less than
- \leq less than or equal to

Interval notation:

- Use square brackets for values that are included
- Use round brackets for values that are not included

Ex. $-3 < x \leq 8$ in interval notation is $(-3, 8]$

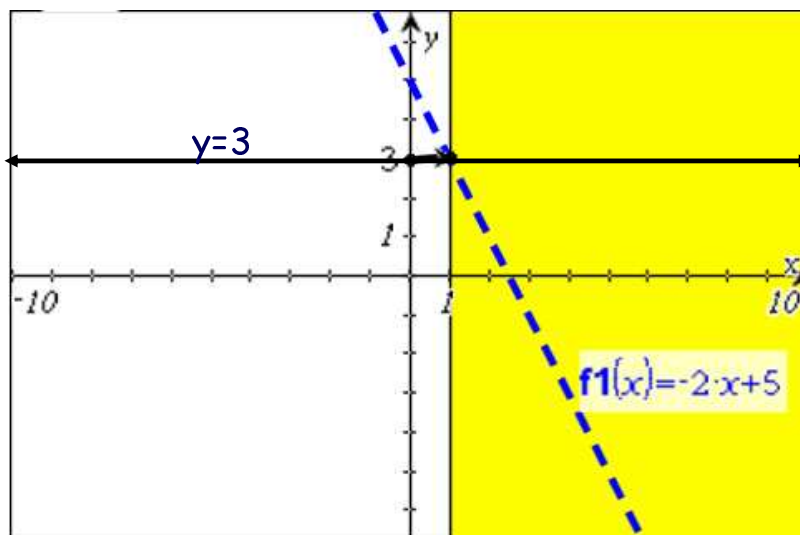
What is the difference between an equation and an inequality?

An equation leads to
one or many solutions which represent **points** on a graph.

An inequality leads to
a solution set - one or more **intervals** of x-values that satisfy the criteria.

Ex. 1 Solve $-2x + 5 < 3$

➔ We want to know the x-values where the graph of $y = -2x + 5$ has a y-value that is less than 3.



$(1, \infty)$

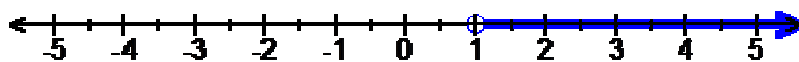
Solution is
 $\{x \in \mathbb{R} \mid x > 1\}$
 or
 $(1, \infty)$

Algebraically:

$$\begin{aligned} -2x + 5 &< 3 \\ -2x &< -2 \\ \frac{-2x}{-2} &> \frac{-2}{-2} && \text{Pull} \\ x &> 1 \end{aligned}$$

Note: When you multiply or divide by a negative, you must change the direction of the inequality.

The solution can be expressed on a number line:



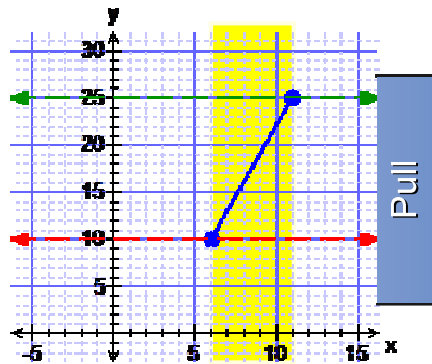
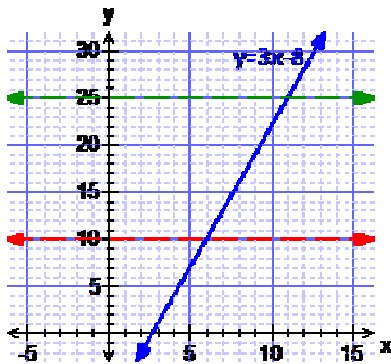
Ex. 2 Solve $10 \leq 3(2x - 5) - (3x - 7) \leq 25$

This is a **double inequality**. The solution must satisfy $10 \leq 3(2x - 5) - (3x - 7)$ **AND** $3(2x - 5) - (3x - 7) \leq 25$

Pull

$$\begin{aligned}
 y &= 3(2x - 5) - (3x - 7) \\
 &= 6x - 15 - 3x + 7 \\
 &= 3x - 8
 \end{aligned}$$

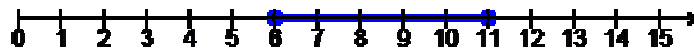
The function defined by $y = 3(2x - 5) - (3x - 7)$ must be greater than or equal to 10 and less than or equal to 25:



You can solve these two inequalities algebraically at the same time:

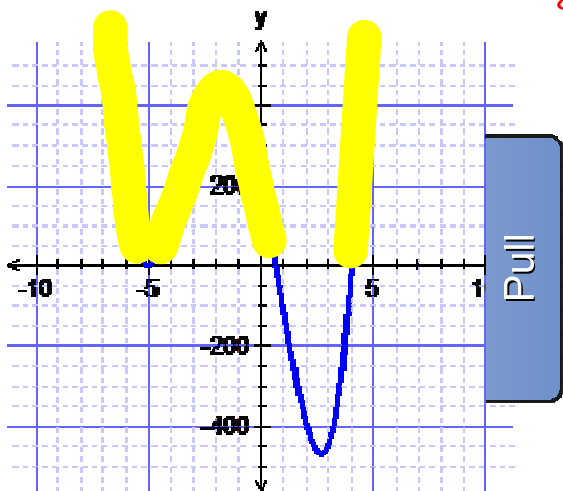
$10 \leq 3(2x - 5) - (3x - 7) \leq 25$	
$10 \leq 6x - 15 - 3x + 7 \leq 25$	← Expand and simplify
$10 \leq 3x - 8 \leq 25$	
$10 + 8 \leq 3x - 8 + 8 \leq 25 + 8$	← Add 8 to all three parts
$18 \leq 3x \leq 33$	
$6 \leq x \leq 11$	← Divide all parts by 3

Expressed on a number line:



Ex. 3 a) Solve $f(x) > 0$, where $f(x) = 3x^4 + 16x^3 - 57x^2 - 270x + 200$, using graphing technology.

zeros: $-5, \frac{2}{3}, 4$



Solution:

$(-\infty, -5)$
 $(-5, \frac{2}{3})$
 $(4, \infty)$

Pull

b) if $f(x) \geq 0$

$\therefore (-\infty, \frac{2}{3}] \cup [4, \infty)$

c) if $f(x) < 0$

$(\frac{2}{3}, 4)$

d) if $f(x) \leq 0$

$[\frac{2}{3}, 4]$

e) How would you solve $f(x) > 0$ algebraically?

Start by factoring....

more later.....

Homework
Page 213 #4de, 5bef, 7ef, 8a, 9, 10, 11

