

## 7.2b Combining Functions

### What did you learn in Lesson 7.2?



**Domain:** The combined function is restricted to the intersection of the domains of  $f(x)$  and  $g(x)$ . *Common Domain*

**Range:** The combined function can be found by combining the y-values for the combined function  $f(x)$  and  $g(x)$ .

Ex 1: If  $f = \{(-3, 2), (5, -10), (0, -3), (6, 1)\}$  and  $g = \{(1, -10), (6, 2), (4, 0), (5, 7)\}$ ,

a) Find the common domain

$$D = \{5, 6\}$$

b) Determine:

i)  $(f \times g)(x)$

$$= f(x)g(x)$$

$$= fg(x)$$

$$= \{(5, -10 \times 7), (6, 1 \times 2)\}$$

$$= \{(5, -70), (6, 2)\}$$

ii)  $(g \div f)(x)$

$$= \frac{g}{f}(x) \text{ OR } = \frac{g(x)}{f(x)}$$

$$= \{(5, \frac{-7}{10}), (6, 2)\}$$

Ex 2: If  $f(x) = \frac{1}{4x-8}$  and  $g(x) = \sqrt{-x+6}$

a) Find the common domain

$D_f \Rightarrow 4x-8=0$   
 $x=2$   
 $x \neq 2$

$D_g \Rightarrow -x+6 \geq 0$   
 $-x \geq -6$   
 $x \leq 6$

$$D = \{x \in \mathbb{R} \mid x \leq 6, x \neq 2\}$$

b) Determine:

i)  $(fg)(x)$

$$= \frac{1}{4x-8} (\sqrt{-x+6})$$

$$= \frac{\sqrt{-x+6}}{4x-8}, x \leq 6 \text{ \& } x \neq 2$$

ii)  $(g \div f)(x)$

$$= \frac{\sqrt{-x+6}}{\frac{1}{4x-8}}$$

$$= \sqrt{-x+6} (4x-8), x \leq 6 \text{ \& } x \neq 2$$

Key Features of Combining Functions:

1) Even/Odd functions

even ± even = even

odd ± odd = odd

even ± odd = neither

odd × odd = even

even × even = even

odd × even = odd

2) Zeros:

a) if you are adding or subtracting a function with a zero, the sum or difference at that x value will be the value (y-value) of the other function

if  $f(x) = 0 \rightarrow f(x) + g(x) = g(x)$

if  $g(x) = 0 \rightarrow f(x) + g(x) = f(x)$

Add/Subtract a zero? DOES NOTHING!

b) if you are multiplying a function with a zero, the product at that x value will have a value (y-value) of zero

if  $f(x)$  or  $g(x) = 0 \rightarrow (f \times g)(x) = 0$

Multiply by a zero? Zero!

c) if you are dividing a function with a zero, the quotient at that x value will have an asymptote.

if  $f(x) = 0 \rightarrow \frac{g(x)}{f(x)} = \text{undef}$

Dividing by a zero? Asymptote!

3) Points of Intersection:

a) subtraction: resultant becomes  $\rightarrow$  y-value is zero.

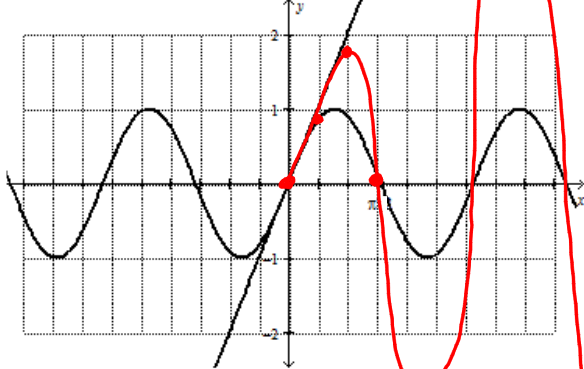
b) addition: resultant becomes  $\rightarrow$  2 x the y-value of Point

c) multiplication becomes  $\rightarrow$  y-value of point is squared

d) division: becomes  $\rightarrow$  + 1

Ex 3: For each of the following examples fill in the tables identifying the key features of the resulting function. State if original and combined functions are even, odd or neither.

a)  $f(x) = \sin x$        $g(x) = x$

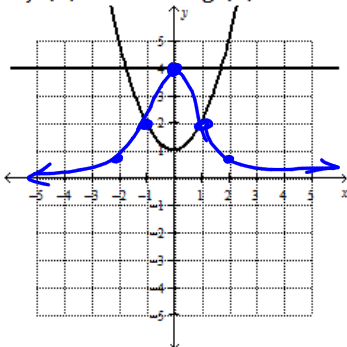


x	f	g	fg
0	0	0	0
$\pi/3$	$\sqrt{3}/2$	1	$\sqrt{3}/2$
$2\pi/3$	$\sqrt{3}/2$	2.1	1.8
$\pi$	0	3.1	0

→ Multiply

ODD \* ODD = EVEN

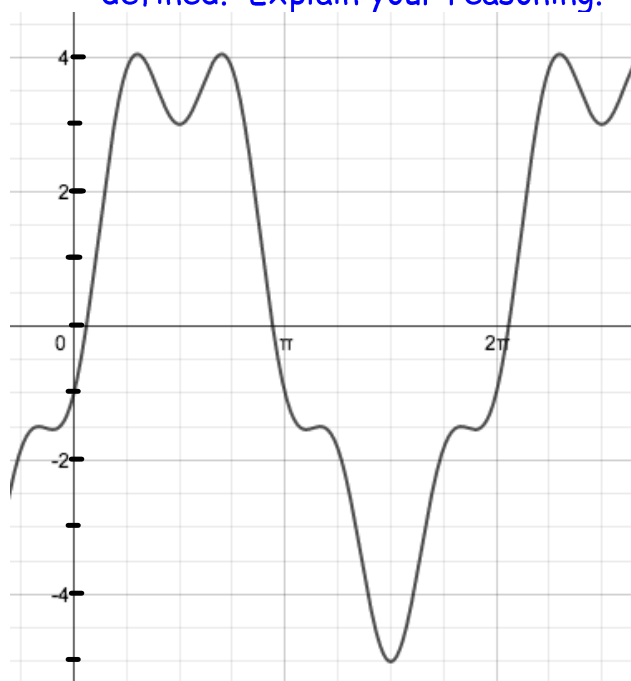
b)  $f(x) = 4$        $g(x) = x^2 + 1$



x	f	g	f ÷ g
-2	4	5	4/5
-1	4	2	2
0	4	1	4
1	4	2	2
2	4	5	4/5

EVEN ÷ EVEN = EVEN

Ex 4: The following function was created by combining two familiar functions. Predict which two functions may have been combined, and how they were defined. Explain your reasoning.



Periodic!  $\sin x$ ?  
Amplitude?  
 $4\sin x$ ?

Translated down?

$$4\sin x - \cos 4x$$

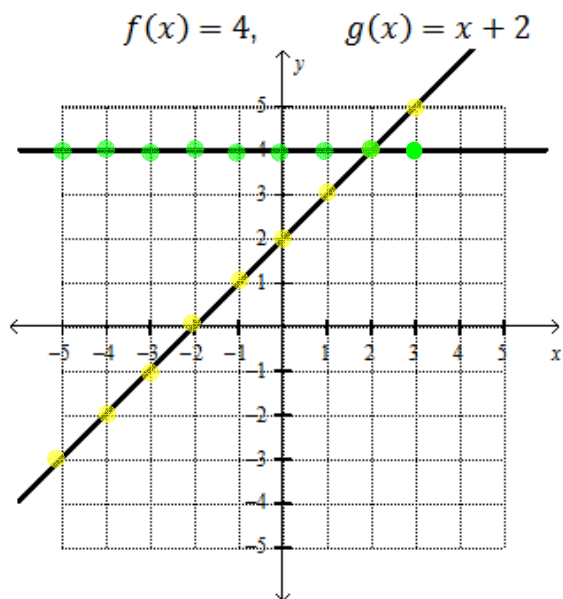
# Homework

p. 528 #2,5,13

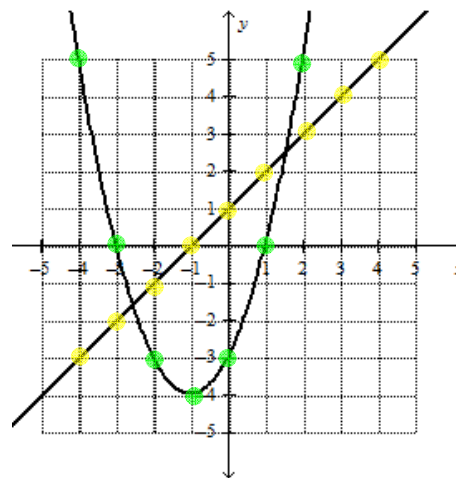
p. 537 #1bf,3,4-7f,10

p. 542 #2 (for #1cdf)

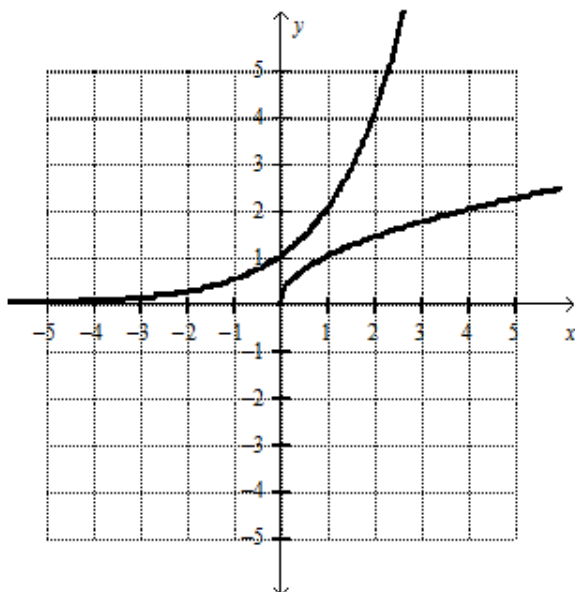




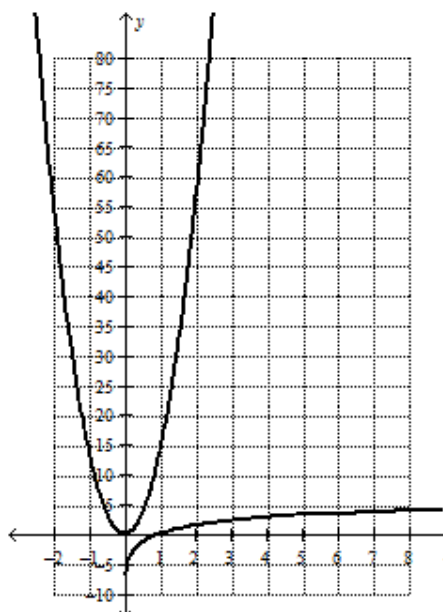
$f(x) = x + 1$        $g(x) = (x + 3)(x - 1)$



$$f(x) = 2^x \quad g(x) = \sqrt{x}$$



$$f(x) = 14x^2 \quad g(x) = 2\log x$$



consider the coordinates:

$(-1, 14), (0, 0), (1, 14)$

$(1, 0), (10, 2)$