

4.1 Multiplying Binomials

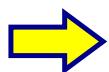
Given a quadratic in vertex form or factored (zeros) form, how could you rewrite it in standard form?

Recall:

vertex form: $y = a(x - h)^2 + k$

factored form: $y = a(x - r)(x - s)$

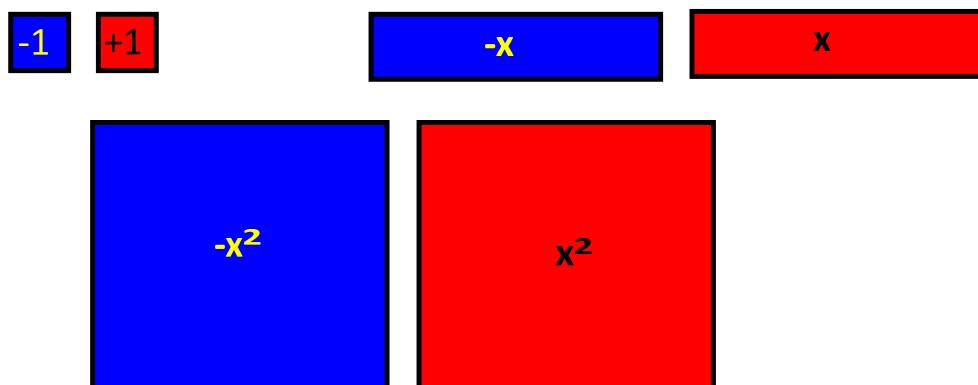
standard form: $y = ax^2 + bx + c$



You need to be able to multiply two binomials together!

Simplifying Polynomials

To simplify polynomials you need to identify like terms (terms with the same variables and exponents)

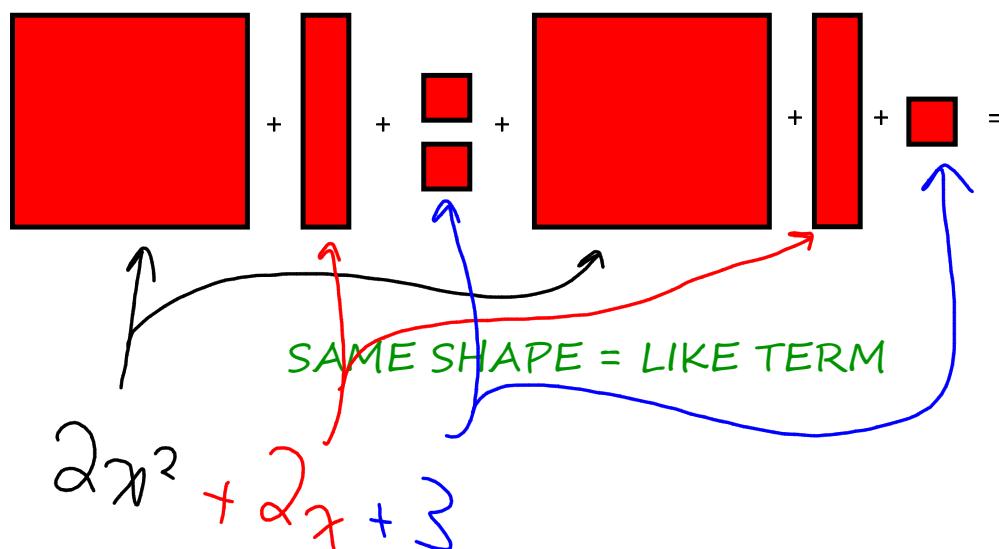


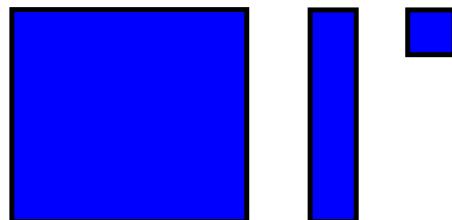
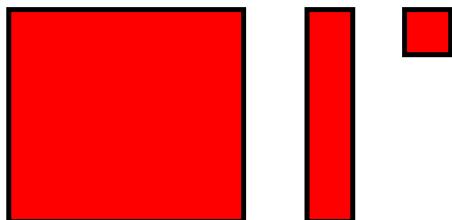
Zero Principle

The diagram shows three examples of the zero principle:

- A large blue square plus a large red square equals 0.
- A long blue rectangle plus a long red rectangle equals 0.
- A small blue square plus a small red square equals 0.

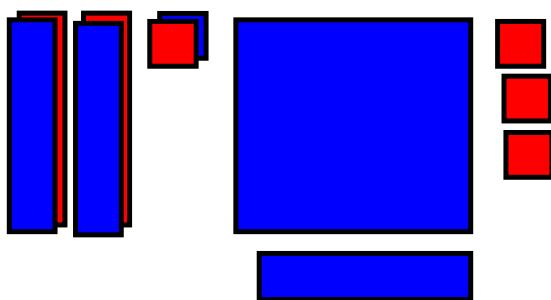
Remember.... you can only add or subtract LIKE TERMS....





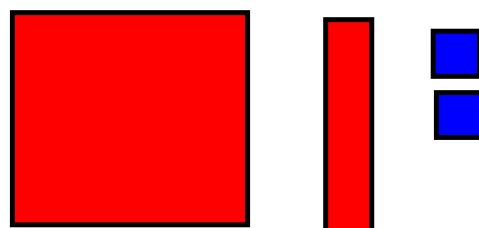
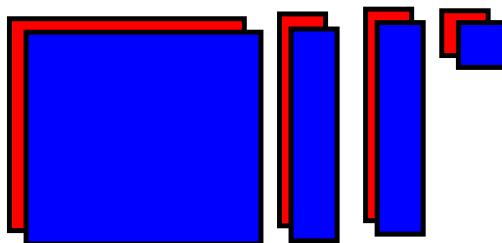
Ex. 1 Represent the simplified expression using alge-tiles

a) $(-x^2 + 2x - 1) + (4 - 3x)$



$$= -x^2 - x + 3$$

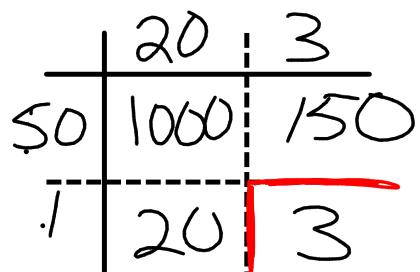
b) $(2x^2 + 3x + 1) + (-x^2 - 2x - 3)$



$$= x^2 + x - 2$$

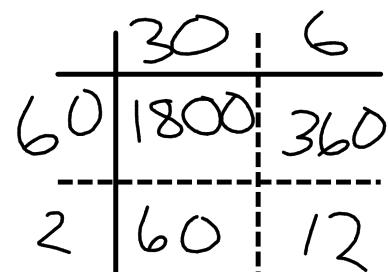
Perform each multiplication without a calculator:

$$23 \times 51$$



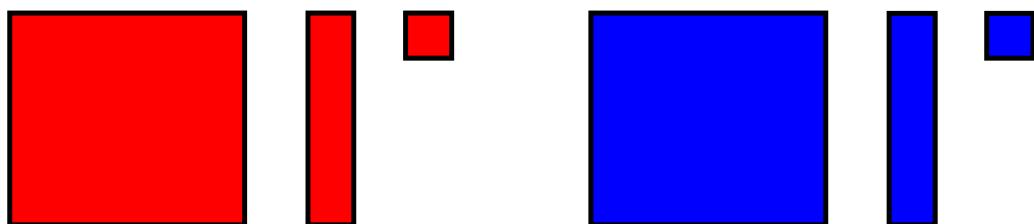
$$\begin{aligned} &= 1000 + 150 + 20 + 3 \\ &= 1173 \end{aligned}$$

$$36 \times 62$$



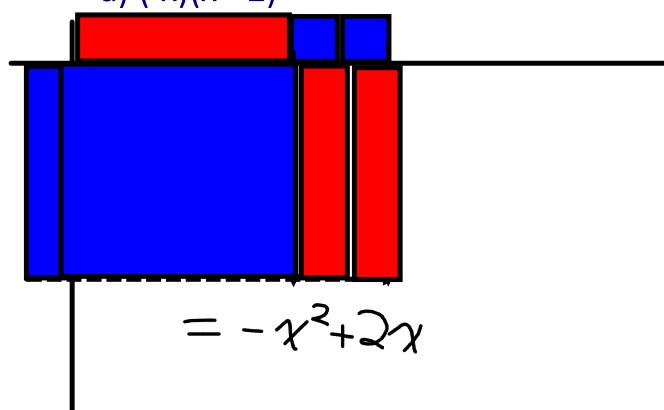
$$\begin{aligned} &= 1800 + 360 + 60 + 12 \\ &= 2232 \end{aligned}$$

This is called an area model.

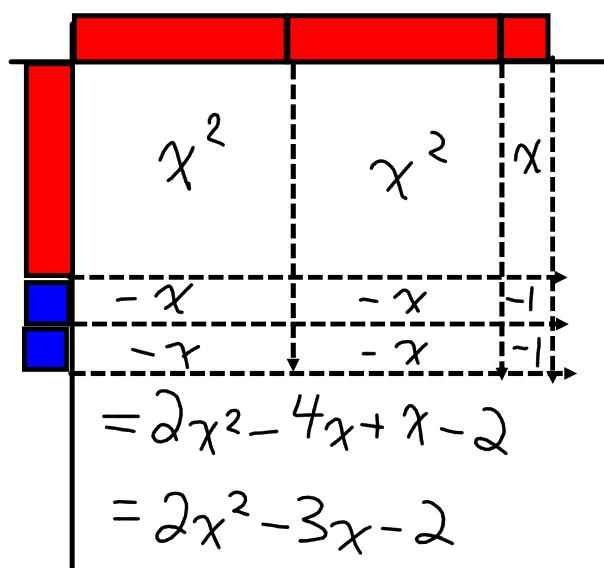


Ex. 2 Use algebra tiles to expand and simplify.

a) $(-x)(x - 2)$



b) $(2x + 1)(x - 2)$



[Video...](#)

$2x$	1
$2x^2$	x
$-4x$	-2

Ex. 3 Use the chart method to expand the following.

a) $(2x^2 - 1)(3 - x^2)$

	3	$-x^2$
$2x^2$	$6x^2$	$-2x^4$
-1	-3	x^2

$$\begin{aligned}
 &= -2x^4 + 6x^2 + x^2 - 3 \\
 &= -2x^4 + 7x^2 - 3
 \end{aligned}$$

b) $(m^2 - 2)(2m + 1)$

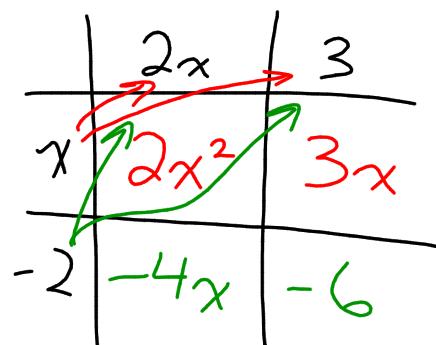
	2m	1
m^2	$2m^3$	m^2
-2	-4m	-2

$$= 2m^3 + m^2 - 4m - 2$$

now... consider the distributive property!

$$\begin{aligned}
 & (x - 2)(2x + 3) = \\
 & = 2x^2 + 3x - 4x - 6 \\
 & = 2x^2 - x - 6
 \end{aligned}$$

$$\begin{aligned}
 & (x - 3)(x + 1) = \\
 & = x^2 + x - 3x - 3 \\
 & = x^2 - 2x - 3
 \end{aligned}$$



Ex. 4 Expand and simplify.

a) $(2x + 1)(x + 4)$

$$\begin{aligned} &= 2x^2 + 8x + x + 4 \\ &= 2x^2 + 9x + 4 \end{aligned}$$

b) $(5 + 2x)(-2 + 3x)$

$$\begin{aligned} &= -10 + 15x - 4x + 6x^2 \\ &= 6x^2 + 11x - 10 \end{aligned}$$

c) $(2q - 3p)(3q + 2p)$

$$\begin{aligned} &= 6q^2 + 4qp - \underbrace{9pq - 6p^2}_{} \\ &= 6q^2 - 5pq - 6p^2 \end{aligned}$$

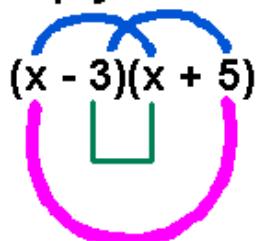
d) $-3(x + 3)(2x + 1)$

$$\begin{aligned} &= -3(2x^2 + x + 6x + 3) \\ &= -3(2x^2 + 7x + 3) \\ &= -6x^2 - 21x - 9 \end{aligned}$$

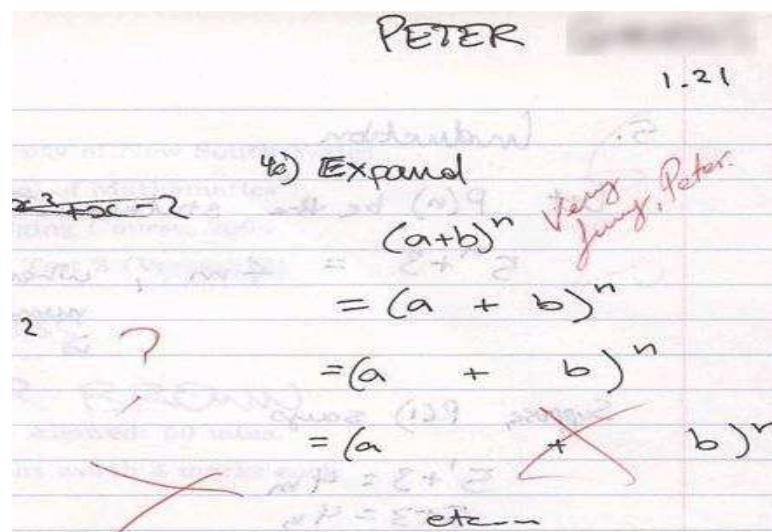
e) $(x^2 - 3x - 4)(2x^2 - 4x + 5)$

$$\begin{aligned} &= \cancel{2x^4} - \cancel{4x^3} + \cancel{5x^2} - \cancel{6x^3} + \cancel{12x^2} - \cancel{15x} - \cancel{8x^2} + \cancel{16x} - 20 \\ &= 2x^4 - 10x^3 + 9x^2 + x - 20 \end{aligned}$$

Multiply:



The Man With
The Big Nose



FBUHL
Page 217
C2, 1, 4aceg, 6acfh, 7acf,
8ace, 9, 10, 14, 16