

**Warmup!***Don't copy - lets do them together!*

Review: tricky negatives ...evaluate each of the following.

a)  $(-2)^4$

$= 16$

b)  $-2^4$

$= -16$

c)  $-3^2$

$= -9$

d)  $(-3)^2$

$= 9$

e)  $-(-5)^2$

$= -25$

$= -(-5)(-5)$

Don't write - just follow.....

Complete the following chart. Evaluate each to standard form. Leave as whole numbers or fractions.

Expression to be Simplified	Write in Expanded Form	Using Exponent Laws
$\frac{2^3}{2^1}$	$= \frac{2 \times 2 \times \cancel{2}}{\cancel{2}}$ $= 4$	$2^{3-1} = 2^2$ $= 4$
$\frac{2^3}{2^2}$	$= \frac{2 \cdot \cancel{2} \cdot \cancel{2}}{\cancel{2} \cdot \cancel{2}} \rightarrow = 2$	$2^{3-2} = 2^1$ $= 2$
$\frac{2^3}{2^3}$	$= \frac{2 \cdot 2 \cdot 2}{2 \cdot 2 \cdot 2}$ $= 1$	$2^{3-3} = 2^0$ $= 1$
$\frac{2^3}{2^4}$	$= \frac{\cancel{2} \cdot \cancel{2} \cdot \cancel{2}}{\cancel{2} \cdot \cancel{2} \cdot \cancel{2} \cdot 2}$ $= \frac{1}{2}$	$2^{3-4} = 2^{-1}$ $= \frac{1}{2}$

Now write...

3.2 Zero and Negative Exponents

Zero Exponents: Any base to the exponent 0 equals 1

ex.  $4^0 = 1$       ex.  $(-3)^0 = 1$

note your BASE cannot be 0

Ex. 1 Evaluate each of the following:

a)  $5^0$

$= 1$

b)  $4^0$

$= 1$

c)  $(-3)^0$

$= 1$

d)  $-4^0$

$= -1$

Negative Exponents:

Any base to a negative exponent ...

invert (flip) the base and make the exponent positive.

$$\begin{aligned} \text{ex. } 4^{-1} &= \left(\frac{4}{1}\right)^{-1} \\ &= \left(\frac{1}{4}\right)^1 \\ &= \frac{1}{4} \end{aligned}$$

$$\begin{aligned} \text{ex. } \left(\frac{1}{3}\right)^{-1} &= \left(\frac{3}{1}\right)^1 \\ &= 3 \end{aligned}$$

$$\begin{aligned} \text{ex. } \left(\frac{3}{4}\right)^{-2} &= \left(\frac{4}{3}\right)^2 \\ &= \frac{4^2}{3^2} \\ &= \frac{16}{9} \end{aligned}$$

Ex. 2 Evaluate. No decimals.

a)  $8^{-2}$

$= \frac{1}{8^2}$

$= \frac{1}{64}$

b)  $(-3)^{-4}$

$= \frac{1}{(-3)^4}$

$= \frac{1}{81}$

c)  $-3^{-2}$

$= -\frac{1}{3^2}$

$= -\frac{1}{9}$

d)  $1^{-7}$

$= \frac{1}{1^7}$

$= 1$

Ex. 3 Evaluate. No decimals.

$$\begin{array}{lll} \text{a) } \left(\frac{1}{4}\right)^{-2} & \text{b) } \left(\frac{2}{5}\right)^{-1} & \text{c) } \left(\frac{3}{7}\right)^{-2} \\ = \left(\frac{4}{1}\right)^2 & = \left(\frac{5}{2}\right)^1 & = \left(\frac{7}{3}\right)^2 \\ = 4^2 & = \frac{5}{2} & = \frac{7^2}{3^2} \\ = 16 & & = \frac{49}{9} \end{array}$$

Ex. 4 Use exponent laws to write as a single power, then evaluate. No decimals.

$$\begin{array}{llll} \text{a) } 5^3 \times 5^{-5} & \text{b) } (2^3)^{-2} & \text{c) } 4^{-3} \div 4^{-5} & \text{d) } \left(\frac{1}{3^2}\right)\left(\frac{1}{3^{-6}}\right) \\ = 5^{3+(-5)} & = 2^{-6} & = 4^{-3-(-5)} & = \frac{1}{3^2 \cdot 3^{-6}} \\ = 5^{-2} & = \frac{1}{2^6} & = 4^{-3+5} & = \frac{1}{3^{2+(-6)}} \\ = \frac{1}{5^2} & = \frac{1}{64} & = 4^2 & = \frac{1}{3^{-4}} \\ = \frac{1}{25} & & = 16 & = 3^4 \\ & & & = 81 \end{array}$$

$$\begin{array}{llll} \text{e) } \frac{7^2}{7^4} & \text{f) } (-2)^3(-2)^{-4} & \text{g) } \frac{12^6}{12^6} & \text{h) } \left(\frac{1}{2}\right)^{-5}\left(\frac{1}{2}\right)^3 \\ = 7^{2-4} & = (-2)^{3+(-4)} & = 12^{6-6} & = \left(\frac{1}{2}\right)^{-5+3} \\ = 7^{-2} & = (-2)^{-1} & = 12^0 & = \left(\frac{1}{2}\right)^{-2} \\ = \frac{1}{7^2} & = -\frac{1}{2} & = 1 & = 2^2 \\ = \frac{1}{49} & & & = 4 \end{array}$$

Ex. 5 Write each number as a power with the stated base

25 (with base of 5)

$$= 5^2$$

32 (with base of 2)

$$= 2^5$$

Ex. 6

Write each numerator and denominator as a power with the same base, then use exponent laws to simplify.

Write your answer as a power with positive exponents.

hint try base of 3

a)  $\frac{64}{16}$

$$= \frac{4^3}{4^2}$$

$$= 4^{3-2}$$

$$= 4$$

b)  $\frac{243}{2187}$

$$= \frac{3^5}{3^7}$$

$$= 3^{5-7}$$

$$= 3^{-2}$$

$$= \frac{1}{3^2}$$

$$= \frac{1}{9}$$

c)  $\frac{1}{25} \times \frac{1}{125}$

$$= 5^{-2} \times 5^{-3}$$

$$= 5^{-2+(-3)}$$

$$= 5^{-5}$$

$$= \frac{1}{5^5}$$

$$= \frac{1}{3125}$$

Practice: page 367

#2<sub>ag</sub>, 3<sub>left column</sub>, 8<sub>left column</sub>

#11<sub>ac</sub>, 12-15, 16<sub>dh</sub>