

1.3 - Binary Point Numbers

and the ASCII Table!

What are they?

Binary point numbers are the way numbers like

42.625

are represented in binary.

But first, we'll start the other way

Take a number like:

$$1101.101_2$$

And remember our columns?

Example: Binary point number to decimal

$$\begin{array}{ccccccc} 2^3 & 2^2 & 2^1 & 2^0 & 2^{-1} & 2^{-2} & 2^{-3} \\ 1 & 1 & 0 & 1 & . & 1 & 0 & 1_2 \\ = 8 & + & 4 & + & 0 & + & 1 & + & 0.5 & + & 0 & + & 0.125 \\ = 13.625_{10} \end{array}$$

You try: Binary point number to decimal

$$\begin{array}{cccccccc} 2^3 & 2^2 & 2^1 & 2^0 & 2^{-1} & 2^{-2} & 2^{-3} & 2^{-4} \\ 1 & 0 & 1 & 1 & . & 0 & 0 & 1 & 1_2 \\ = 8 & + & 0 & + & 2 & + & 1 & + & 0 & + & 0 & + & 0.125 & + & 0.0625 \\ = 11.1875_{10} \end{array}$$

And finally the reverse

Rules:

- Use only the fractional part (to the right of the decimal)
- Multiply by 2
- Take the fractional part and repeat until the fractional part is zero.
- Read the numbers DOWNWARD

ex: 0.375_{10} to binary

$$\begin{array}{l} 0.375 \quad * 2 = 0.75 \\ 0.75 \quad * 2 = 1.5 \\ 0.5 \quad * 2 = 1.0 \\ \\ = 0.011_2 \end{array}$$

Another Example

Convert 42.125_{10} to binary

1 $42_{10} = 101010_2$
the usual way (div by 2)

2 $0.125 * 2 = 0.25$
 $0.25 * 2 = 0.5$
 $0.5 * 2 = 1.0$

$= 101010.001_2$

Sometimes it gets funky...

Convert 0.4_{10} to binary

$= 0.0110011001100..._2$

$= \overline{0.0110}_2$

0.4	* 2 = 0.8
0.8	* 2 = 1.6
0.6	* 2 = 1.2
0.2	* 2 = 0.4
0.4	* 2 = 0.8
0.8	* 2 = 1.6
0.6	* 2 = 1.2
.....	

Practice

- Convert the following to their decimal equivalents.
 - 10.01_2
 - 101.101_2
 - 1010.1001_2
 - 101.0011_2
- Convert to binary
 - 8.375
 - 13.5625
 - 9.875
 - 8.1875
- Convert to binary
 - 1.1
 - 2.2
 - 3.3
 - 4.4

Dec	Hx	Oct	Char	Dec	Hx	Oct	Html	Chr	Dec	Hx	Oct	Html	Chr	Dec	Hx	Oct	Html	Chr
0	0	000	NUL (null)	32	20	040	 	Space	64	40	100	@	@	96	60	140	`	`
1	1	001	SOH (start of heading)	33	21	041	!	!	65	41	101	A	A	97	61	141	a	a
2	2	002	STX (start of text)	34	22	042	"	"	66	42	102	B	B	98	62	142	b	b
3	3	003	ETX (end of text)	35	23	043	#	#	67	43	103	C	C	99	63	143	c	c
4	4	004	EOT (end of transmission)	36	24	044	$	\$	68	44	104	D	D	100	64	144	d	d
5	5	005	ENQ (enquiry)	37	25	045	%	%	69	45	105	E	E	101	65	145	e	e
6	6	006	ACK (acknowledge)	38	26	046	&	&	70	46	106	F	F	102	66	146	f	f
7	7	007	BEL (bell)	39	27	047	'	'	71	47	107	G	G	103	67	147	g	g
8	8	010	BS (backspace)	40	28	050	((72	48	110	H	H	104	68	150	h	h
9	9	011	TAB (horizontal tab)	41	29	051))	73	49	111	I	I	105	69	151	i	i
10	A	012	LF (NL line feed, new line)	42	2A	052	*	*	74	4A	112	J	J	106	6A	152	j	j
11	B	013	VT (vertical tab)	43	2B	053	+	+	75	4B	113	K	K	107	6B	153	k	k
12	C	014	FF (NP form feed, new page)	44	2C	054	,	,	76	4C	114	L	L	108	6C	154	l	l
13	D	015	CR (carriage return)	45	2D	055	-	-	77	4D	115	M	M	109	6D	155	m	m
14	E	016	SO (shift out)	46	2E	056	.	.	78	4E	116	N	N	110	6E	156	n	n
15	F	017	SI (shift in)	47	2F	057	/	/	79	4F	117	O	O	111	6F	157	o	o
16	10	020	DLE (data link escape)	48	30	060	0	0	80	50	120	P	P	112	70	160	p	p
17	11	021	DC1 (device control 1)	49	31	061	1	1	81	51	121	Q	Q	113	71	161	q	q
18	12	022	DC2 (device control 2)	50	32	062	2	2	82	52	122	R	R	114	72	162	r	r
19	13	023	DC3 (device control 3)	51	33	063	3	3	83	53	123	S	S	115	73	163	s	s
20	14	024	DC4 (device control 4)	52	34	064	4	4	84	54	124	T	T	116	74	164	t	t
21	15	025	NAK (negative acknowledge)	53	35	065	5	5	85	55	125	U	U	117	75	165	u	u
22	16	026	SYN (synchronous idle)	54	36	066	6	6	86	56	126	V	V	118	76	166	v	v
23	17	027	ETB (end of trans. block)	55	37	067	7	7	87	57	127	W	W	119	77	167	w	w
24	18	030	CAN (cancel)	56	38	070	8	8	88	58	130	X	X	120	78	170	x	x
25	19	031	EM (end of medium)	57	39	071	9	9	89	59	131	Y	Y	121	79	171	y	y
26	1A	032	SUB (substitute)	58	3A	072	:	:	90	5A	132	Z	Z	122	7A	172	z	z
27	1B	033	ESC (escape)	59	3B	073	;	;	91	5B	133	[[123	7B	173	{	{
28	1C	034	FS (file separator)	60	3C	074	<	<	92	5C	134	\	\	124	7C	174	|	
29	1D	035	GS (group separator)	61	3D	075	=	=	93	5D	135]]	125	7D	175	}	}
30	1E	036	RS (record separator)	62	3E	076	>	>	94	5E	136	^	^	126	7E	176	~	~
31	1F	037	US (unit separator)	63	3F	077	?	?	95	5F	137	_	_	127	7F	177		DEL

Source: www.LookupTables.com