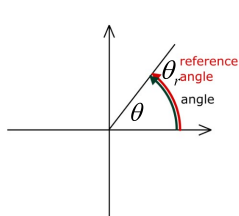


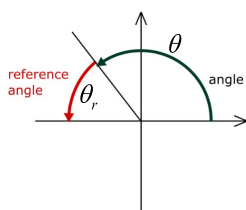
Lesson 4.1B: Angles between 0° and 360° (Day 2)

Recall:



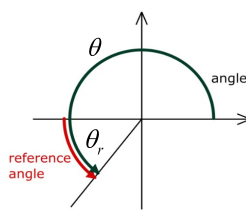
I quadrant

$$\theta_r = \theta$$



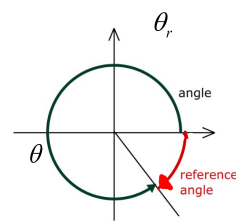
II quadrant

$$\theta_r = 180 - \theta$$



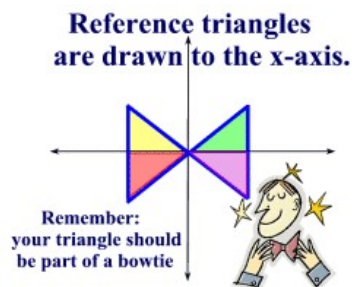
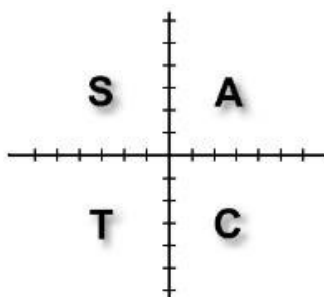
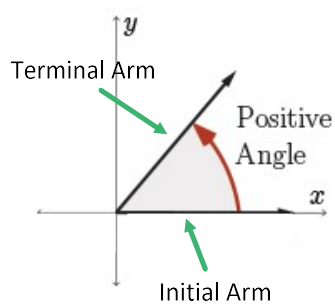
III quadrant

$$\theta_r = \theta - 180$$



IV quadrant

$$\theta_r = 360 - \theta$$



Lesson 4.1B: Angles between 0° and 360° (Day 2)

Ex. 1: Determine all angles between 0° and 360° that have the following trig ratios. Include a diagram.

a) $\sin A = -0.4752$

$$A = \sin^{-1}(-0.4752)$$

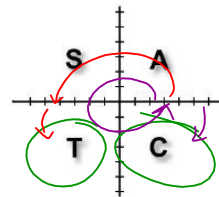
$$\approx -28^\circ$$

$$\theta_r = 28^\circ$$

Sine is negative
in which quadrants?

NOTE

Calc will always
try to give
smallest #



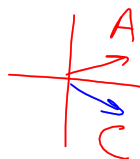
Sine is negative

$$\begin{array}{c} \text{Q3} \\ \theta = 180 + 28 \\ = 208^\circ \end{array}$$

$$\begin{array}{c} \text{Q4} \\ \theta = 360 - 28 \\ = 332^\circ \end{array}$$

$$\therefore \theta = 208^\circ, 332^\circ$$

b) $\cos A = \frac{1}{3}$



$$A = \cos^{-1}\left(\frac{1}{3}\right)$$

$$\approx 71^\circ$$

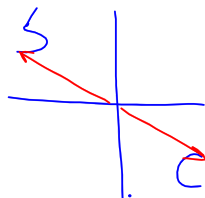
$$\theta_r = 71^\circ$$

$$\begin{array}{c} \text{Q1} \\ \theta = 71^\circ \end{array}$$

$$\begin{array}{c} \text{Q4} \\ \theta = 360 - 71 \\ = 289^\circ \end{array}$$

$$\therefore \theta = 71^\circ, 289^\circ$$

c) $\tan \theta = -2.14$



$$\theta = \tan^{-1}(-2.14)$$

$$\approx -65^\circ$$

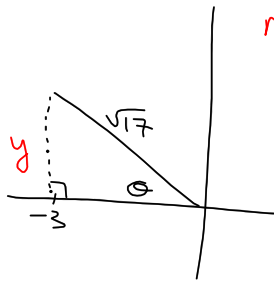
$$\theta_r = 65^\circ$$

$$\begin{array}{c} \text{Q2} \\ \theta = 180 - 65^\circ \\ = 115^\circ \end{array}$$

$$\begin{array}{c} \text{Q4} \\ \theta = 360 - 65^\circ \\ = 295^\circ \end{array}$$

$$\therefore \theta = 115^\circ, 295^\circ$$

Ex. 2: If $\cos \theta = -\frac{3}{\sqrt{17}}$ where $90^\circ < \theta < 180^\circ$, determine $\sin \theta$ and $\tan \theta$.



Need y in order
to list other ratios

$$\begin{aligned} r^2 &= x^2 + y^2 \\ (\sqrt{17})^2 &= (-3)^2 + y^2 \\ y^2 &= 17 - 9 \\ y &= \sqrt{8} \\ &= 2\sqrt{2} \end{aligned}$$

$$\begin{aligned} \sin \theta &= \frac{2\sqrt{2}}{\sqrt{17}} \cdot \frac{\sqrt{17}}{\sqrt{17}} \\ &= \frac{2\sqrt{34}}{17} \end{aligned}$$

$$\begin{aligned} \tan \theta &= \frac{2\sqrt{2}}{-3} \\ &= -\frac{2\sqrt{2}}{3} \end{aligned}$$