

1.0 Prerequisite Skills for Unit 1

Linear Relations

1. Graph each of the following lines:

a) $y = -x + 5$

b) $3x + 5y - 15 = 0$

c) $x = -4$

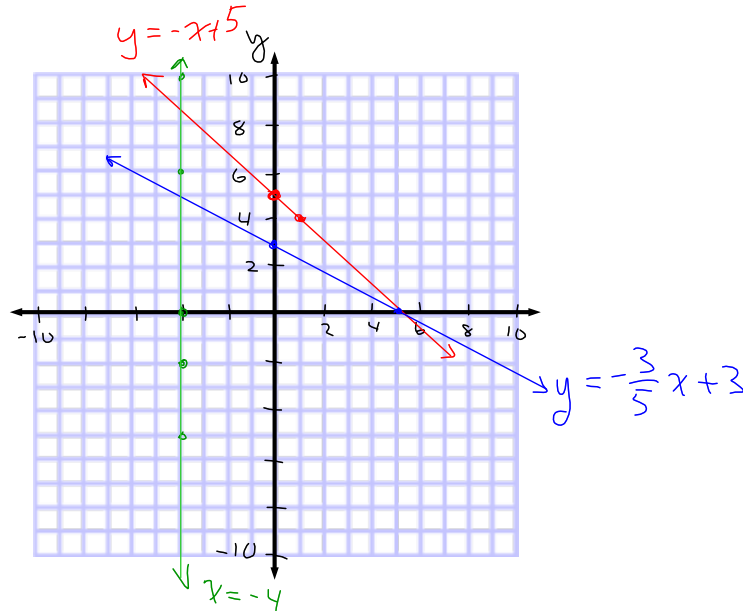
$$y = mx + b$$

$$5y = -3x + 15$$

$$y = -\frac{3}{5}x + 3$$

$$m = -\frac{1}{1}$$

$$b = 5$$



2. Determine the equation in slope y-intercept form of a line passing through the points $(-2, 5)$ and $(6, -1)$.

$$y = mx + b$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\text{Sub } m = -\frac{3}{4}$$

$$= \frac{-1 - 5}{6 - (-2)}$$

$$y = -\frac{3}{4}x + b$$

$$= \frac{-6}{8}$$

$$\text{Sub in } (-2, 5)$$

$$5 = -\frac{3}{4}(-2) + b$$

$$= -\frac{3}{4}$$

$$5 = \frac{3}{2} + b$$

$$\therefore y = -\frac{3}{4}x + \frac{7}{2}$$

$$\frac{10}{2} - \frac{3}{2} = b$$

$$\frac{7}{2} = b$$

3. Use the methods of substitution and elimination to solve the following linear system: $y = 2x + 1$ and $x + 2y = 7$

Substitution

$$\textcircled{1} y = 2x + 1$$

$$\textcircled{2} x + 2y = 7$$

Sub $\textcircled{1}$ into $\textcircled{2}$

$$x + 2(2x + 1) = 7$$

$$x + 4x + 2 = 7$$

$$5x = 5$$

$$x = 1$$

Sub $x = 1$ into $\textcircled{1}$

$$y = 2(1) + 1$$

$$= 3$$

$$\therefore (1, 3)$$

Elimination

$$2x - y = -1$$

$$x + 2y = 7 \quad \times 2$$

$$2x - y = -1$$

$$2x + 4y = 14 \quad -$$

$$0 - 5y = -15$$

$$y = 3$$

Sub $y = 3$ into $x + 2y = 7$

$$x + 2(3) = 7$$

$$x = 1$$

$$\therefore (1, 3)$$

Working with Polynomials

1. Expand and simplify.

$$(a+b)^2 = a^2 + 2ab + b^2$$

a) $(x-3)(x+8)$

$$= x^2 + 8x - 3x - 24$$

$$= x^2 + 5x - 24$$

b) $(x+5)^2$

$$= x^2 + 10x + 25$$

c) $(x-10)(x+10)$

$$= x^2 - 100$$

2. Factor completely.

a) $x^2 + x - 30$

$$= (x-5)(x+6)$$

M -30

A 1

N -5, 6

b) $4x^2 - 36$

c) $12x^2 + 5x - 3$

$$= (2x-6)(2x+6)$$

M 5

N 9, -4

$$12x^2 + 9x - 4x - 3$$

$$= 3x(4x+3) - 1(4x+3)$$

$$= (4x+3)(3x-1)$$

d) $49x^2 - 28x + 4$

Perfect Square!

$$= (7x-2)^2$$

3. What value of k makes this quadratic expression a perfect square trinomial?

$$= (x-10)^2$$

$$x^2 - 20x + k$$

$$20x = 2ab$$

$$10x = ab$$

$$a = x$$

$$10x = x b$$

$$10 = b$$

$$(a+b)^2 = a^2 + 2ab + b^2$$

4. Factor out the coefficient of the quadratic term of the following polynomial:

$$-\frac{3}{5}x^2 - 6x$$

$$-6 \div -\frac{3}{5}$$

$$= -\frac{3}{5}(x+10x)$$

$$= -\cancel{6}^2 \times -\frac{5}{\cancel{3}_1}$$

$$= \frac{30}{3}$$

$$= 10$$

Quadratic Relations

1. For the given quadratic relation, state:

- a) the coordinates of the vertex
- b) the equation of the axis of symmetry
- c) the direction of opening
- d) the y-intercept

Then, sketch a graph of the relation.

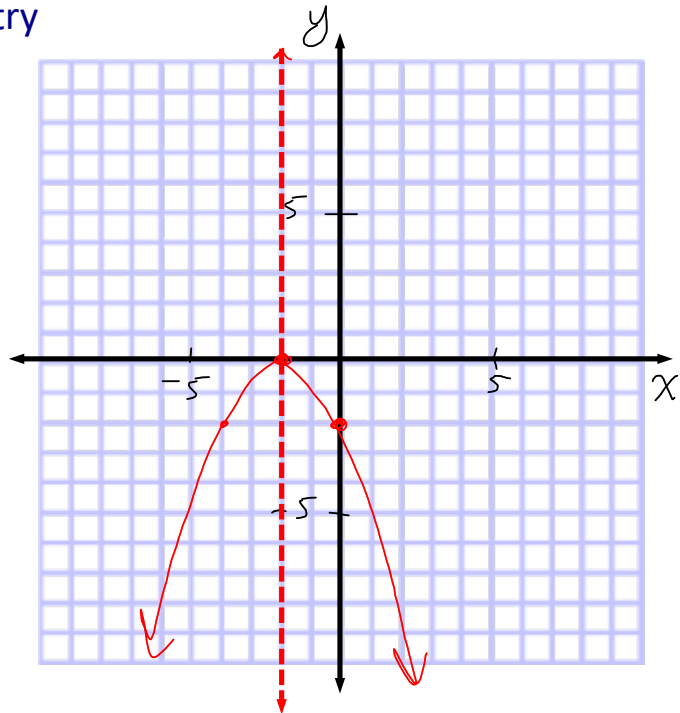
$$y = -\frac{1}{2}(x+2)^2$$

a) $V(-2, 0)$

b) $x = -2$

c) $a < 0$
 \therefore DOWN

d) Sub $x = 0$
 $y = -\frac{1}{2}(4)$
 $= -2$



2. Complete the square in order to express the following quadratic relation in vertex form:

$$y = x^2 - 6x + 2$$

$$\begin{aligned} y &= x^2 - 6x + 9 - 9 + 2 \\ &= (x - 3)^2 - 7 \end{aligned}$$

Homework

- pg. 2 #1 - 15
- Pick and choose for the remainder of class - focus on what you find hardest!