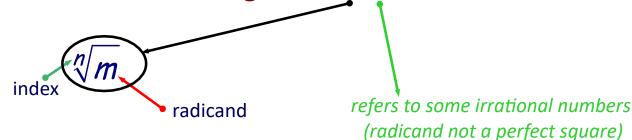
Lesson 1.5A Working With Radicals



Properties of Radicals:

1) Multiplication

In general:
$$\sqrt{b} \cdot \sqrt{d}$$
 $\sqrt{b} \cdot \sqrt{d}$ \sqrt{d} $\sqrt{$

2) Division

$$\sqrt{\frac{81}{9}} \qquad \boxed{\frac{\sqrt{81}}{\sqrt{9}}} \\
= \sqrt{9} \qquad \boxed{\frac{9}{3}} \\
= 3 \qquad \boxed{\frac{9}{3}}$$

In general:

$$\frac{\sqrt{b}}{\sqrt{d}} \qquad \frac{a\sqrt{b}}{c\sqrt{d}}$$

$$= \sqrt{\frac{b}{d}} \qquad = \sqrt{\frac{b}{d}}$$

3) Squaring

$$(\sqrt{b})^{2} \qquad (a\sqrt{b})^{2}$$

$$= b \qquad = a^{2}(\sqrt{b})^{2}$$

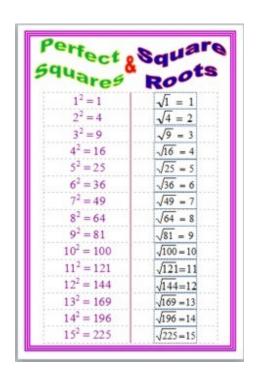
$$= a^{2}b$$

$$= a^{2}b$$

In general:

$$\left(a\sqrt{b}\right)^{m}$$

$$= Q^{m}\left(\sqrt{b}\right)^{m}$$



Radicals can be: Entire or \sqrt{n} $a\sqrt{b}$

Sometimes entire radicals can be changed to mixed radicals by simplifying.

Ex. 1 Change Entire Radicals to Mixed Radicals TWO

a)
$$\sqrt{27}$$
 b) $\sqrt{48}$ c) $\sqrt{500}$ d) $\sqrt{180}$

$$= \sqrt{9.3} = \sqrt{16}\sqrt{3} = \sqrt{36}\sqrt{5}$$

$$= \sqrt{9}\sqrt{3} = 4\sqrt{3} = 10\sqrt{5} = 6\sqrt{5}$$

$$= 3\sqrt{3}$$

A radical is in simplest form if:

- 1. The radical has no perfect square factors other than 1 in the radicand.
- 2. There are no fractions under a $\sqrt{.}$ $\sqrt{\frac{1}{6}}$
- 3. There are no $\sqrt{\ }$ in the denominator. $\frac{1}{\sqrt{2}}$

Multiplying and Dividing Radicals:

Ex. 2 Simplify.

a)
$$\sqrt{5} \cdot \sqrt{7}$$

$$= \sqrt{35}$$

b)
$$3\sqrt{6} \cdot \sqrt{2}$$

= $3\sqrt{12}$
= $3\sqrt{4}\sqrt{3}$
= $6\sqrt{3}$

c)
$$(5\sqrt{6})(2\sqrt{8})$$

= $10\sqrt{48}$ = $10\sqrt{6}\sqrt{3}$
= $40\sqrt{3}$ = $10.4\sqrt{3}$
= $40\sqrt{3}$

d)
$$(2\sqrt{6})(3\sqrt{2})(5\sqrt{6})$$

= $2\cdot 3\cdot 5\sqrt{6\cdot 2\cdot 6}$
= $30\sqrt{72}$
= $30\sqrt{36\cdot 2}$
= $180\sqrt{2}$

e)
$$\sqrt{3}(\sqrt{6}+5)$$

$$= \sqrt{18} + \sqrt{15}$$

$$= 3\sqrt{2} + \sqrt{15}$$

f)
$$\frac{\sqrt{18}}{\sqrt{3}}$$
 = $\sqrt{\frac{18}{3}}$

g)
$$\frac{15\sqrt{7}}{3\sqrt{4}} = \frac{\sqrt{4}}{\sqrt{4}}$$

$$= \frac{\sqrt{5}\sqrt{28}}{\sqrt{3}\sqrt{4}}$$

$$= \frac{\sqrt{5}\sqrt{7}}{\sqrt{7}}$$

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$$= \frac{\sqrt{5}\sqrt{7}}{\sqrt{7}}$$

h)
$$\frac{5\sqrt{12}}{\sqrt{8}} \cdot \frac{\sqrt{8}}{\sqrt{8}}$$

$$= \frac{5\sqrt{96}}{8}$$

$$= \frac{5\sqrt{16 \cdot 6}}{8}$$

$$= \frac{5\sqrt{16 \cdot 6}}{8}$$

$$= \frac{5\sqrt{16}}{8}$$

Rationalizing the Denominator

Multiply both the numerator and the denominator by the radical in the denominator.

Squaring the radical will eliminate it from the denominator.

Adding and Subtracting Radicals:

Algebra: Collect like terms.

Like Terms

Same variables, same exponents

3x, 4x**Example:**

Counter-example: $2\chi^2$

Radicals: Collect like radicals.

Like Radicals

Same index, same radicand

Example: $\sqrt{3}$ $4\sqrt{3}$

Counter-example: 2\overline{3}, 2\overline{5}

Ex. 3 Are the following radicals like or unlike?

a)
$$2\sqrt{3}, -3\sqrt{3}, 4\sqrt{3}$$

a)
$$2\sqrt{3}, -3\sqrt{3}, 4\sqrt{3}$$
 b) $\sqrt{4}, \sqrt{2}, \sqrt{3}$ c) $\sqrt{8}, \sqrt{2}, \sqrt{32}$ d) $\sqrt[3]{3}, \sqrt{3}, \sqrt[4]{3}$

d)
$$\sqrt[3]{3}$$
, $\sqrt{3}$, $\sqrt[4]{3}$

LIKE UNLIKE

Ex. 4 Add or Subtract.

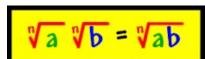
a)
$$\sqrt{27} + \sqrt{20} - \sqrt{12} + \sqrt{45}$$

a)
$$\sqrt{27} + \sqrt{20} - \sqrt{12} + \sqrt{45}$$
 b) $7\sqrt{2} - 6\sqrt{63} - \sqrt{28} + 5\sqrt{18}$

$$=22\sqrt{2}-20\sqrt{7}$$

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$$\frac{\sqrt[n]{a}}{\sqrt[n]{b}} = \sqrt[n]{\frac{a}{b}}$$

You CANNOT split up the radical across a + or – sign.

$$\sqrt{x+y} \neq \sqrt{x} + \sqrt{y}$$
$$\sqrt{x-y} \neq \sqrt{x} - \sqrt{y}$$