#### Lesson 2.3B: Horizontal and Vertical Translations of Functions

## **Part A: Vertical Translations**

Using Desmos, describe the transformations to the base graph in each case.

Graph a couple of equations at a time so that you can see the transformation from the base function.

a) 
$$f(x) = x^2$$

BASE FUNCTION

b) 
$$g(x) = f(x) + 5$$

b) g(x) = f(x) + 5 graph moves  $\bigcirc \bigcirc \bigcirc$ 

c) 
$$h(x) = f(x) - 3$$

c) h(x) = f(x) - 3 graph moves  $\bigcirc$ 

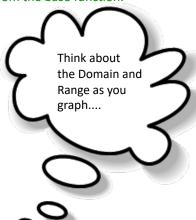
$$d) f(x) = \sqrt{x}$$

e) 
$$g(x) = f(x) + 4$$

d)  $f(x) = \sqrt{x}$  BASE FUNCTION e) g(x) = f(x) + 4 graph moves

$$f) h(x) = f(x) - 2$$

f) h(x) = f(x) - 2 graph moves



Try graphing the base function along with each of these:

g) 
$$m(x) = \frac{1}{x} + 3$$

g)  $m(x) = \frac{1}{x} + 3$  Base Function:  $\frac{1}{x}$  graph moves  $\bigcirc \bigcirc$ 

h) 
$$n(x) = x^3 - 5$$

h)  $n(x) = x^3 - 5$  Base Function:  $\chi$  3 graph moves  $\chi$ 

**General Result** 

g(x) = f(x) + c is a vertical transfation of the graph of f(x).

If c > 0, the graph of f(x) moves  $\cup P \subset \cup \cap \overline{\downarrow}$ If c < 0, the graph of f(x) moves down c with

The domain <u>does not change</u>. The range <u>can c</u> x-values are <u>unaffected</u>. y-values are <u>affected</u>.

c is OUTSIDE of the function so no x-values change.

### **Part B - Horizontal Translations**

Graph the following using Desmos and compare to the base function.

- 1. Graph  $f(x) = x^2$  and the equations below. Describe the transformations.

  - a) g(x) = f(x+4) LEFT 4 b) h(x) = f(x-2) RIGHT 2
- 2. Graph  $f(x) = \sqrt{x}$  and the equations below. Describe the transformations.

  - a) g(x) = f(x+1) LEFT | County 4

General Result g(x) = f(x - d) is A hor 30 tell + 30 tell 40 of the graph of f(x).**General Result** If d > 0, the graph of f(x) moves RIGHT D onits

If d < 0, the graph of f(x) moves

LEFT D units The domain <u>Can-Change</u>. The range <u>does</u> ist <u>change</u> x-values are <u>affected</u>. y-values are <u>not affected</u>

This transformation is the opposite of what you think because the x-coord must compensate for its change in order for the y-coord to stay the same.

d is  $\frac{100 \le 100}{100}$  the function so no y-values change.

# Ex. 1: Given the graph of f(x) shown below, graph:

**Graphing Process** 

- Plot 3 to 5 base points from the parent function.
- Transform these points in order to create the graph.

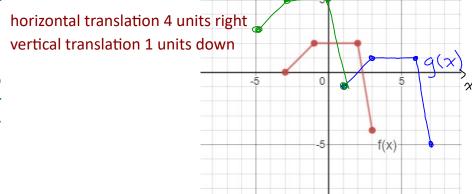
• Use mapping notation to find the coordinates of the transformed points.

a) g(x) = f(x-4)-1



- b) h(x) = f(x+2)+3
  - h.t. 2 units left
  - v.t. 3 units up





Mapping Notation  $(x,y) \rightarrow (x+d,y+c)$ 

$$(x,y) \rightarrow (x+d,y+c)$$

Ex. 2: Find the equation of g(x) = f(x+1) - 3 if:

a) 
$$f(x) = x^2$$
 2  
  $f(x+1) - 3 = (x+1) - 3$ 

a) 
$$f(x) = x^2$$
 b)  $f(x) = x^3$   $f(x+1)-3 = (x+1)^3 - 3$ 

c) 
$$f(x) = \sqrt{x}$$

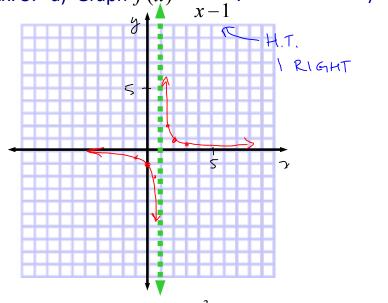
$$d) \quad f(x) = \frac{1}{x}$$

c) 
$$f(x) = \sqrt{x}$$
  
 $f(x+1) - 3 = \sqrt{x+1} - 3$ 

$$f(x+1)-3 = \frac{1}{x+1} - 3$$

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Ex. 3: a) Graph  $f(x) = \frac{1}{x-1}$ .



b) State the domain and range.

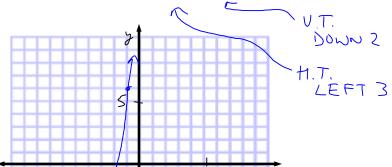
$$D: \{x \in R \mid x \neq 0\}$$

$$R: \{y \in R \mid y \neq 0\}$$

$$D: \left\{ x \in \mathbb{R} \left| x \neq 1 \right. \right\}$$

b) Graph  $f(x) = (x+3)^3 - 2$ .





 $D: \{x \in R\} \checkmark$   $R: \{y \in R\} \checkmark$ 

# HOMEWORK p. 51 #1 p. 70 # 7a, &a, 10ab

# + Extra Practice Sheet 2.3B

