

4.2 Multiplying Binomials & Factoring by Grouping

A. Multiplying Two Binomials using Box Method

1. $(x+y)(a+b)$
 $= ax + bx + ay + by$

	a	b
x	ax	bx
y	ay	by

2. $(x+2)(y-3)$
 $= xy + 2y - 3x - 6$

	y	-3
x	xy	-3x
2	2y	-6

3. $(3x-4)(5y+z)$
 $= 15xy + 3xz - 20y - 4z$

	5y	z
3x	15xy	3xz
-4	-20y	-4z

4. $(2x^2y-1)(3xy+7)$
 $= 6x^3y^2 - 3xy + 14x^2y - 7$

	2x ² y	-1
3xy	6x ³ y ²	-3xy
7	14x ² y	-7

5. $(2-x)(7+3y)$
 $= 14 + 6y - 7x - 3xy$

	7	3y
2	14	6y
-x	-7x	-3xy

6. $(5x-3w)(2j-3k)$
 $= 10jx - 15kw - 6jw + 9kw$

7. $(2x^5y^3 - 3xy^3)(x - 2y)$
 $= 2x^6y^3 - 4x^5y^4 - 3x^2y^3 + 6xy^4$

8. $(5a+2b)(4w-7k)$
 $= 20aw - 35ak + 8bw - 14bk$

B. Factoring by Grouping

1. $ax + ay + bx + by$
 $= (a+b)(x+y)$

	x	y
a	ax	ay
b	bx	by

2. $8x - 12xy - 6 + 9y$
 $= (4x-3)(2-3y)$

	2	$-3y$
$4x$	$8x$	$-12xy$
-3	-6	$9y$

3. $xy - 7x - 3y + 21$
 $= x(y-7) - 3(y-7)$
 $= (y-7)(x-3)$

4. $4x^2y^3 - 2xy^2 + 6xy - 3$
 $= (2xy^2+3)(2xy-1)$

	$2xy^2$	-1
$2xy^2$	$4x^2y^3$	$-2xy^2$
3	$6xy$	-3

5. $3(4x-1) + 5y(4x-1)$
 $= (4x-1)(3+5y)$

6. $2(x^2+x+1) - 5y(x^2+x+1)$
 $= (x^2+x+1)(2-5y)$

7. $4ax - 3by + 2bx - 6ay$
 $= 4ax + 2bx - 3by - 6ay$
 $= 2x(2a+b) - 3y(b+2a)$
 $= 2x(2a+b) - 3y(2a+b)$
 $= (2a+b)(2x-3y)$

8. $10x^4y^2 - 5x^2y + 4x^2y - 2$
 $= 5x^2y(2x^2y-1) + 2(2x^2y-1)$
 $= (2x^2y-1)(5x^2y+2)$

9. $15vx - 6vy + 5wx - 2wy$
 $= (5x-2y)(3v+w)$

	$5x$	$-2y$
$3v$	$15vx$	$-6vy$
w	$5wx$	$-2wy$

10. $2x^2y - 3xy + 4y - 4x^2 + 6x - 8$
 $= (y-2)(2x^2-3x+4)$

	$2x^2$	$-3x$	4
y	$2x^2y$	$-3xy$	$4y$
-2	$-4x^2$	$6x$	-8

Homework

Set 1: Handout #1bdf, 2ace, 3abcdef

Set 2: Handout #2abcdef, 4abcdef