

4.5 Multiplying & Factoring with GCF

How do you multiply 3 numbers together?

$$\begin{aligned} &\widehat{2(3)}(4) \\ &= 6(4) \\ &= 24 \end{aligned}$$

$$\begin{aligned} &\widehat{(4)(-2)}(5) \\ &= (-8)(5) \\ &= -40 \end{aligned}$$



A. Multiplying 3 Factors Together

$$\begin{aligned} 1. & \quad \widehat{4(2x-3)}(w-3y) \\ &= (8x-12)(w-3y) \\ &= 8wx - 12w - 24xy + 36y \end{aligned}$$

$$\begin{aligned} 2. & \quad -3x(a-b)(3c+2d) \\ &= (-3ax+3bx)(3c+2d) \\ &= -9acx - 6adx + 9bcx + 6bdx \end{aligned}$$

	$8x$	-12
w	$8wx$	$-12w$
$-3y$	$-24xy$	$36y$

$$\begin{aligned} 3. & \quad -2(x+3)(x-5) \\ &= (-2x-6)(x-5) \\ &= -2x^2 + 4x + 30 \end{aligned}$$

$$\begin{aligned} 4. & \quad 5(x-4)(x-6) \\ &= (5x-20)(x-6) \\ &= 5x^2 - 30x - 20x + 120 \\ &= 5x^2 - 50x + 120 \end{aligned}$$

	x	-5
$-2x$	$-2x^2$	$10x$
-6	$-6x$	30

$$\begin{aligned} 5. & \quad -x^2(x+2)(x+1) \\ &= (-x^3-2x^2)(x+1) \\ &= -x^4 - 3x^3 - 2x^2 \end{aligned}$$

$$\begin{aligned} 6. & \quad 3(2x-1)(3x+4) \\ &= 3(6x^2+8x-3x-4) \\ &= 3(6x^2+5x-4) \\ &= 18x^2+15x-12 \end{aligned}$$

	x	1
$-x^3$	$-x^4$	$-x^3$
$-2x^2$	$-2x^3$	$-2x^2$

$$7. \quad -5(3x+1)(2x+5)$$

$$8. \quad 4x(3x-4)(2x-3)$$

B. Factoring with a GCF (Greatest Common Factor)

Look for GCF first!!!

1. $3ax - 3ay + 3bx - 3by$
 $= 3(ax - ay + bx - by)$
 $= 3(a+b)(x-y)$

	x	$-y$
a	ax	$-ay$
b	bx	$-by$

2. $-12x^2y - 8x^2 + 6xy + 4x$
 $= -2x(6xy + 4x - 3y - 2)$
 $= -2x[2x(3y+2) - 1(3y+2)]$
 $= -2x(3y+2)(2x-1)$

3. $5x^2 - 5x - 60$
 $= 5(x^2 - x - 12)$
 $= 5(x-4)(x+3)$

$M - 12$
 $A - 1$
 $N - 4, 3$

	x	-4
x	x^2	$-4x$
3	$3x$	-12

Look for GCF first!!!

4. $-2x^2y + 10xy - 12y$
 $= -2y(x^2 - 5x + 6)$
 $= -2y(x-2)(x-3)$

5. $24x^2 + 52x + 20$
 $= 4(6x^2 + 13x + 5)$
 $= 4(3x+5)(2x+1)$

$M 30$
 $A 13$
 $N 10, 3$

	$3x$	5
$2x$	$6x^2$	$10x$
1	$3x$	5

6. $6x^3 + 27x^2 - 15x$
 $= 3x(2x^2 + 9x - 5)$
 $= 3x[2x^2 - x + 10x - 5]$
 $= 3x[x(2x-1) + 5(2x-1)]$
 $= 3x(2x-1)(x+5)$

$M - 10$
 $A 9$
 $N - 1, 10$

7. $6x^4 + 2x^3 - 4x^2$

8. $3x^3y + 6x^2y + 24xy$
 $= 3xy(x^2 + 2x + 8)$
 $= 3xy(\dots \text{not factorable})$
 $= 3xy(x^2 + 2x + 8)$

$M 8$
 $A 2$
 $N ?$

Look for GCF first!!!

$\frac{8}{1, 8}$
 $2, 4$
 $?$