

4.7 Multiplying & Factoring Perfect Square Trinomials

A. Multiplying a Squared Binomial (perfect square)

1. $(x+5)(x+5)$
 $= x^2 + 10x + 25$

	x	5
x	x^2	$5x$
5	$5x$	25

2. $(x-3)(x-3)$
 $= x^2 - 3x - 3x + 9$
 $= x^2 - 6x + 9$



3. $(2x+1)(2x+1)$
 $= 4x^2 + 4x + 1$

	$2x$	1
$2x$	$4x^2$	$2x$
1	$2x$	1

4. $(2x+3)^2 = (2x+3)(2x+3)$
 $= 4x^2 + 6x + 6x + 9$
 $= 4x^2 + 12x + 9$



5. $(4x-1)^2$
 $= 16x^2 - 8x + 1$

	$4x$	-1
$4x$	$16x^2$	$-4x$
-1	$-4x$	1

6. $(3x+5)^2$
 $= 9x^2 + 30x + 25$

7. $(2x-3y)^2$
 $= 4x^2 - 12xy + 9y^2$

8. $(2x+3y)^2$
 $= 4x^2 + 12xy + 9y^2$



9. $(5x^2-2z^3)^2$
 $= 25x^4 - 20x^2z^3 + 4z^6$

10. $(x+4x^2y)^2$
 $= x^2 + 8x^3y + 16x^4y^2$

B. Factoring a Perfect Square Trinomial

$$\text{perfect square} \rightarrow \square^2 + 2\square\{\} + \{\}^2 \leftarrow \text{perfect square}$$

square root of first term square root of second term

1. $x^2 - 4x + 4 = (x - 2)^2$

$\sqrt{x^2} = x$ $\sqrt{4} = 2$

$(x)(-2)(-2) = -4x$ ✓ yes

2. $x^2 + 14x + 49 = (x + 7)^2$

Look for patterns!!!

$(x)(7)(7) = 14x$ ✓ yes

3. $4x^2 - 4x + 1 = (2x - 1)^2$

$\sqrt{4x^2} = 2x$ $\sqrt{1} = 1$

4. $25x^2 + 20x + 4 = (5x + 2)^2$

Look for patterns!!!

5. $9x^2 + 24x + 16 = (3x + 4)^2$

6. $4x^2 - 20x + 25 = (2x - 5)^2$

7. $9x^2 - 42xy + 49y^2 = (3x - 7y)^2$

Look for patterns!!!

8. $x^2y^2 + 6xyz + 9z^2 = (xy + 3z)^2$

9. $16x^4 - 8x^2y + y^2 = (4x^2 - y)^2$

Look for patterns!!!

10. $4a^6 + 12a^3b + 9b^2 = (2a^3 + 3b)^2$
