

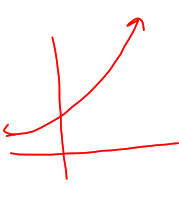
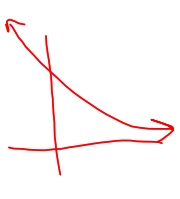
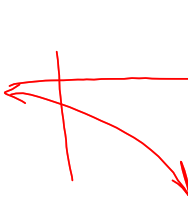
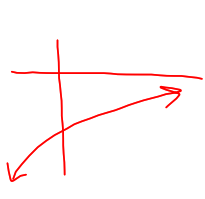
### 3.4 Properties of Exponential Functions

$$f(x) = ab^x$$

Investigate with Desmos and note how the exponential function changes as the base "b" and initial value "a" changes.

Look for:

- ★ The location of the x and y intercepts?
- ★ The location of the horizontal asymptote?
- ★ The Domain and Range

	$a > 0, b > 1$ $a = 3$ $b = 2$	$a > 0, 0 < b < 1$ $a = 3$ $b = \frac{1}{2}$	$a < 0, b > 1$ $a = -3$ $b = 2$	$a < 0, 0 < b < 1$ $a = -3$ $b = \frac{1}{2}$
Transformations	Base $y = 2^x$ V.S. of 3	V.S. by a	Verl. Refl. V.S. by a	V. Refl. V.S. by a
Domain	$\{x \in \mathbb{R}\}$	$\{x \in \mathbb{R}\}$	$\{x \in \mathbb{R}\}$	$\{x \in \mathbb{R}\}$
Range	$\{y \in \mathbb{R} \mid y > 0\}$	$\{y \in \mathbb{R} \mid y > 0\}$	$\{y \in \mathbb{R} \mid y < 0\}$	$\{y \in \mathbb{R} \mid y < 0\}$
x-int	none	none	none	none
y-int --> f(0)	a	a	a	a
Horizontal Asymptote	$y = 0$	$y = 0$	$y = 0$	$y = 0$
Growth or Decay	GROWTH	DECAY		
Sketch				

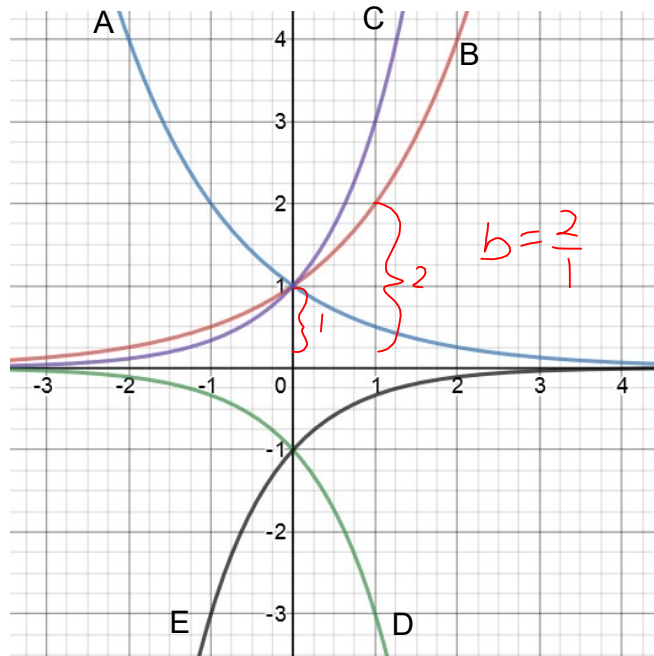
Ex.2 Match the graph with the equation.  
There are extra equations.

$y=2^x$  B       $y=3^x$  C

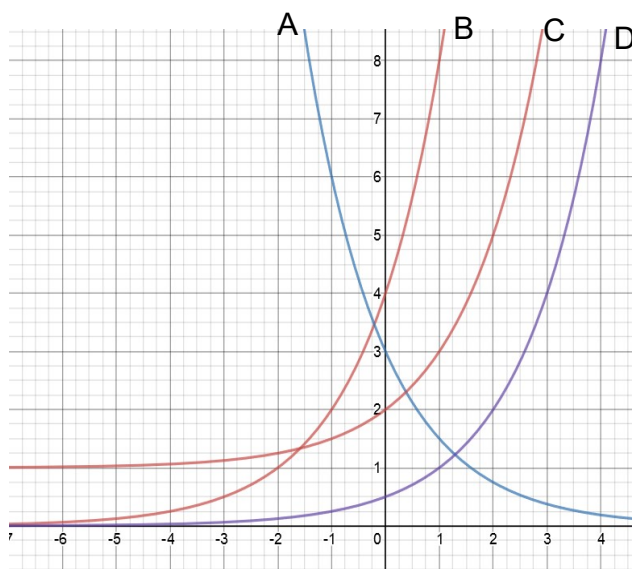
$y=-3^x$  D       $y=-2^x$  A

$y=\left(\frac{1}{2}\right)^x$  A       $y=-\left(\frac{1}{2}\right)^x$  D

$y=\left(\frac{1}{3}\right)^x$  A       $y=-\left(\frac{1}{3}\right)^x$  E



Ex. 3



Match the graph with the equation.  
There are extra equations.

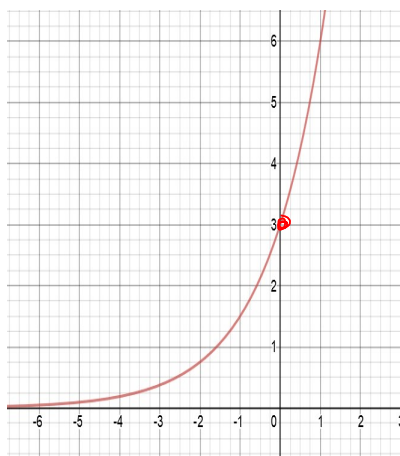
$y = 4(2)^x$  B       $y = 2^x + 1$  C

$y = \frac{1}{2}(2)^x$  D       $y = 3\left(\frac{1}{2}\right)^x$  A  
 (Same eq<sup>n</sup>)  
 $y = 2^{x-1}$  D       $y = (-6)^x$     

$y = 4\left(\frac{1}{2}\right)^x$     

$2^{-1} 2^x$   
 $= \frac{1}{2} 2^x$   
 $= 2^{x-1}$

Ex.4 Write an equation to represent the following graph




$a = 3$      $y$ -int  
 $b = 2$   
 $\therefore y = 3 \cdot 2^x$

## Homework

Pg. 185 # 1,3,4,5,7ac,10

“The greatest shortcoming of the human race is our inability to understand the exponential function.”



**Al Bartlett**  
Professor of Physics  
University of Colorado

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